Trajectory tracking control of agricultural vehicles based on disturbance test

Zhengduo Liu$^{1,2}$, Wenxiu Zheng$^{1,2}$, Neng Wang$^3$, Zhaqin Lyu$^{1,2}$, Wanzhi Zhang$^{1,2*}$

(1. College of Mechanical and Electronic Engineering, Shandong Agricultural University, Taian 271018, Shandong, China; 2. Shandong Provincial Key Laboratory of Horticultural Machinery and Equipment, Taian 271018, Shandong, China; 3. College of Physics and Electronic Science, Hunan University of Science and Technology, Xiangtan 411201, Hunan, China)

Abstract: To improve the trajectory tracking robust stability of agricultural vehicles, a path tracking control method combined with the characteristics of agricultural vehicles and nonlinear model predictive control was presented. Through the proposed method, the path tracking problem can be divided into two problems with speed and steering angle constraints: the trajectory planning problem, and the trajectory tracking optimization problem. Firstly, the nonlinear kinematics model of the agricultural vehicle was discretized, then the derived model was inferred and regarded as the prediction function plant for the designed controller. Second, the objective function characterizing the tracking performance was put forward based on system variables and control inputs. Therefore, the objective function optimization problem, based on the proposed prediction equation plant, can be regarded as the nonlinear constrained optimization problem. What’s more, to enhance the robust stability of the system, a real-time feedback and rolling adjustment strategy was adopted to achieve optimal control. To validate the theoretical analysis before, the Matlab simulation was performed to investigate the path tracking performance. The simulation results show that the controller can realize effective trajectory tracking and possesses good robust stability. Meanwhile, the corresponding experiments were conducted. When the test vehicle tracked the reference track with a speed of 3 m/s, the maximum lateral deviation was 13.36 cm, and the maximum longitudinal deviation was 34.61 cm. When the added horizontal deviation disturbance $\Delta r$ was less than 1.5 m, the controller could adjust the vehicle quickly to make the test car return to the reference track and continue to drive. Finally, to better highlight the controller proposed in this paper, a comparison experiment with a linear model predictive controller was performed. Compared to the conventional linear model predictive controller, the horizontal off-track distance reduced by 36.8% and the longitudinal deviation reduced by 32.98% when performing circular path tracking at a speed of 3 m/s.

Keywords: path tracking, nonlinearity, controller, robustness

DOI: 10.25165/j.ijabe.2020302.4506


1 Introduction

The trajectory tracking of agricultural machinery is the key technology to realize the automation and intelligence of agricultural machinery. The difficulty of path tracking lies in the complicated working environment and the agricultural machinery can difficulty exercise sound judgment. At present, the autonomous driving of small agricultural transport vehicles has made great progress in the indoor field[1-4]. However, affected by natural environment (slope, ground obstacle, surface condition, climate condition) and other factors, outdoor agricultural transport vehicles are difficult to ensure the accuracy and robustness of trajectory tracking[5]. With the development of control theory, domestic and foreign scholars have made some relevant studies on the trajectory tracking of agricultural vehicles[10-12]. Machine vision can collect a lot of path information. It can identify crop rows with image processing technology and then determine navigation datum to realize navigation of agricultural machinery. In response to the problem of autonomous walking of agricultural robots in the field, Sun[13] designed modern seedling recognition and path tracking control systems using modern image processing technology, which can plan walking paths and control the tracking paths of agricultural robots. Wu et al.[14] proposed a dual-view-window path tracking method for AGV station identification and path tracking. Experiments showed that the method improved the real-time and robustness of path feature recognition. In the environment, the average feature recognition accuracy is 99.5%. In view of the navigation problem of agricultural transport vehicles in arched sheds, Li et al.[15] used the chroma method to segment crops and roads to improve the accuracy and real-time performance of path tracking. The average deviation of recognition is 2.4 cm and the detection speed is 240 ms/f. Machine vision is greatly affected by lighting in outdoor conditions. Meanwhile, due to a large number of images need to be processed, the real-time is poor. With the development of GPS technology, RTK-DGPS high-precision automatic navigation system has been widely used in practical agricultural production[16-18]. Luo et al.[19] adopted the RTK-DGPS positioning technology to design the automatic navigation system of the Dongfenghong X-804 tractor and verified the accuracy and reliability of the control system through field
experiments. Erkan et al.\textsuperscript{[20]} designed the fuzzy control path tracking controller based on the nonlinear least square method and developed the navigation control system based on GNSS, but it had large tracking error in experiment. This was because the tree branches and leaves occlusion signal receiver, so that the signal receiver cannot receive the satellite signal stably, resulting in a large deviation. Li et al.\textsuperscript{[21,22]} designed an automatic navigation system based on the combination of RTK-DGPS positioning and dual closed-loop steering control. The method for improving the precision of navigation control of agricultural machinery was studied. Experiments showed that the average value of path tracking error does not exceed 0.019 m and the standard deviation does not exceed 0.041 m.

Thus it can be seen that due to the complexity of the working environment (branches and leaves of the trees keep out signal, high temperature, dust, ground inequality), agricultural machinery relies on external positioning makes the positioning inaccurate and the robustness poor\textsuperscript{[23-25]}.

To solve the above problems, this paper combines the model predictive control and agricultural transport vehicle to design navigation controller to realize the trajectory tracking of agricultural vehicles. Model predictive control is widely used in automatic vehicle navigation\textsuperscript{[26,27]}, active front wheel steering\textsuperscript{[28,29]} and other aspects. It can make up for the uncertainty caused by model mismatch, time change and interference. Felix et al.\textsuperscript{[30]} based on the analytical model predictive control theory, combined with the nonlinear model predictive control, designed a kind of ship positioning control system. It can make the ship move rapidly to the reference position. Velenis et al.\textsuperscript{[31]} designed a trajectory tracking controller based on a predictive control method taking the frictional limit of the tires of an autonomous vehicle into consideration. Due to the complexity of the coupled nonlinear model, the calculation time was too long, which did not achieve good results in practical real-time applications. In this paper, a nonlinear model predictive control algorithm is proposed and adopted. Compared with linear model predictive controllers, the model accuracy is improved. Meanwhile, the computational complexity is reduced and the path tracking performance is increased.

2 Path tracking system structure

The designed field tracking test vehicle is shown in Figure 1, the related structural parameters in Table 1.

\begin{table}[h]
\centering
\begin{tabular}{|l|c|}
\hline
Technical index & Parameters \\
\hline
Dimension LxWxH/cm & 120x63x33 \\
Wheelbase/cm & 100 \\
Maximum speed/m s\textsuperscript{-1} & 3.2 \\
Weight/kg & 50 \\
Control method & PWM \\
Tire radius/cm & 15 \\
\hline
\end{tabular}
\caption{Main technical indexes of the autonomous vehicle system}
\end{table}

The main parts include a path information acquisition module, an E6B2-CCWZ3E type angle encoder sensor with a measurement error of ±0.3°, a JK5002D Hall speed sensor with speed error of ±0.05 m/s, a control execution module, and a path information processing module.

The front-wheel steering driver is the ASMT-01 series high-power linear servo controller. The front-wheel steering actuator is a 42BYGH47 step with a stroke of 80 mm and a maximum speed of 29 mm/s. The rear-wheel drive is a CM2010 brushless motor controller. The rear-wheel actuator is a DMW86 brushless DC motor with a rated speed of 3200 r/min and a rated power of 1000 W.

Path information processing module is a navigation controller comprised of a STM32F103ZET6 type microcontroller. The main task is to collect the information from the speed sensor and the front-wheel angle sensor of the tested vehicle. The information is sent to host computer via WIFI and processed by Matlab software. Its structure and function are shown in Figure 2.
3 Kinematic model of agricultural vehicles

The kinematics analysis of agricultural vehicles is carried out and the kinematics model shown in Figure 3 is established in the plane coordinate system. The front wheel of the model turns and rear wheel drive. In the process of work, the steering wheel and the driving wheel adjust the angle and speed by adjusting the voltage. In the whole kinematics analysis, the agricultural vehicle is regarded as a rigid body running on horizontal plane. In order to determine the agricultural vehicle’s position and attitude in the whole trajectory, the navigation coordinate is set up. The center point of the test car’s rear axle was selected as a reference point to define the position and position information of the car.

Pose information is defined as \((x, y, \phi)\). In which, \(x, y\) are the axial coordinates of the vehicle’s rear axle (m); \(\phi\) is the heading angle (rad); \(l\) is the distance between the front and rear axles (m); \(v\) is the speed of agricultural vehicles at moment \(k\), m/s; \(\delta\) is the front wheel Angle of the agricultural vehicle at moment \(k\), rad;

According to this mathematic model, it is necessary to know the initial pose information \((x(k), y(k), \phi(k))\) of the controlled system at a certain time and the control input sequence \((v_1, \delta_1), (v_2, \delta_2)\) to predict the output sequence of the system in the predicted \(k+1\) time domain. Equation (3) is sorted into the form of output function:

\[
\begin{align*}
\eta_j(t + j|t) &= F_j(\zeta(t|t), u(t|t), \ldots, u(t + N_i - 1|t)) \\
(j & = 1, 2, \ldots, N_p)
\end{align*}
\]

where, \(N_p\) is predicted time domain; \(N_i\) is controlled time domain.

To reduce the computational complexity and enhance the real-time performance of the control system. This paper \(N_p=2\), thus, the prediction model of nonlinear model predictive controller is obtained:

\[
\begin{align*}
\hat{F}_p(t) = \begin{bmatrix}
\eta_1(t + 1|t) \\
\eta_1(t + 2|t) \\
\vdots \\
\eta_1(t + N_p|t)
\end{bmatrix} = \begin{bmatrix}
F_1(\cdot) \\
F_2(\cdot) \\
\vdots \\
F_{N_p}(\cdot)
\end{bmatrix}, \quad j = 1, 2, \ldots, N_p
\end{align*}
\]

4 Design of nonlinear model predictive controller

4.1 Prediction model

In the nonlinear model predictive control, the traditional algorithm has the problem of large computation and slow convergence. This paper use an explicit iterative equation by using Euler method to solve the discretization of the kinematics model. So the convergence rate of the system is accelerated by decreasing the computation.

\[
\begin{align*}
x(k + 1) &= x(k) + T v \cos(\phi(k + 1)) \\
y(k + 1) &= y(k) + T v \sin(\phi(k + 1)) \\
\phi(k + 1) &= \phi(k) + \frac{T v \tan(\delta)}{l} \\
\end{align*}
\]

where, \(k\) is a discrete time variable; \((x(k), y(k))\) is the axial coordinates of agricultural vehicles at moment \(k\), m; \(\phi(k)\) is the heading angle at moment \(k\), rad; \(v\) is the speed of agricultural vehicles at moment \(k\), m/s; \(\delta\) is the front wheel Angle of the agricultural vehicle at moment \(k\), rad;

4.2 Closed-loop correction for nonlinear models

In order to improve the robust performance of the control system, closed-loop correction of the prediction model is coined based on the error prediction and real-time feedback.

\[
e(t + i - 1|t) = \Gamma_r(t + i - 1|t) - \Gamma_r(t + i - 1|t)
\]

where, \(e(t+i-1|t)\) is the error of the system at \(t+i-1\) based on the real-time information measurement at \(t\); \(\Gamma_r(t+i-1|t)\) is the system output at \(t+i-1\) based on the real-time information measurement at \(t\). \(\Gamma_r(t+i-1|t)\) is the output at \(t+i-1\) based on kinematics model of the agricultural vehicle at \(t\). \(\Gamma_i(t) = [\eta_1(t+1|t), \ldots, \eta_1(t+N_p|t)]^T, i = 1, 2, \ldots, N_p\)

\[
\begin{align*}
\eta_1(t + 1|t) &= X_1(t) + T v \cos(\phi(t + 1)) \\
y_1(t + 1|t) &= Y_1(t) + T v \sin(\phi(t + 1)) \\
\phi_1(t + 1|t) &= \phi_1(t) + \frac{T v \tan(\delta)}{l} \\
\end{align*}
\]
where, $\Delta u$ is the input control variable, which is used to limit the variation of the control amount; $\Delta \Gamma$ is the lateral deviation, which is used to limit and minimize the lateral deviation; the relaxation factor $\varepsilon$ is used to control the change of the variable each iteration, which mainly affects the convergence speed and convergence of the iteration. In some cases, the smaller the relaxation factor, the smaller the change between two iterations.

$$\Delta \Gamma(i) = \Gamma(i) - \Gamma(i)$$

$$= \left[ e(t + 1) - e(t + 1) \right] \ldots \left[ e(t + 1) - e(t + 1) \right]$$

(9)

The path tracking problem is transformed to solve the constraint problem of nonlinear quadratic form by setting the value range of state quantity and control quantity. Both the objective function and the constraint function are continuous, and the gradient is continuous in Equation (8). Therefore, the objective optimization problem can be solved based on quadratic programming of the recursive sequence. Taking the nonlinear boundary constraints into account, the optimization problem can be summarized as

$$J = \sum_{i=1}^{N_c} \Delta \Gamma(i) + \sum_{i=1}^{N_c} \Delta u(i) + \rho \varepsilon^2$$

(8)

s.t.

$$\Gamma_{\min} \leq \Gamma(i) \leq \Gamma_{\max}$$

$$\Delta \Gamma_{\min} \leq \Delta \Gamma(i) \leq \Delta \Gamma_{\max}$$

$$u_{\min} \leq u(i) \leq u_{\max}(k = 0, 1, \ldots, N_r - 1)$$

$$\Delta u_{\min} \leq \Delta u(i) \leq \Delta u_{\max}(k = 0, 1, \ldots, N_r - 1)$$

(10)

5 Simulation result and analysis

5.1 Test site

Figure 4 is the experiment place in the plum forest of Shandong Agricultural University and Figure 5 shows the reference trajectory of the agricultural driverless vehicle traveling from point O to point G.

Figure 4 Forest of Shandong reference path

The agricultural vehicle starts from the O point to G point for the end. Where $A(X_0, 0), B(20, 1), C(22.5), D (10.3, 5), E(0.5), F(-2.9), G(20, 9)$. The tracking performance can be evaluated by the parameters observed at these points. Point A is defined as the maximum overshoot point at the transient response during vehicle path tracking. Point D is defined as the disturbance test point and additional disturbance is added to test the robustness of the nonlinear model predictive controller. The model predictive controller is designed in Matlab platform. The simulation analysis is carried out from these four aspects: forward speed $v$, sampling period $T$, lateral deviation disturbance $Y$, and front wheel corner disturbance $\psi$.

Figure 5 Experiment path trajectory

The controller parameters are set according to the path information (the reference path coordinate range and the parameter range of the front-wheel steering angle when the car is turning) and the target speed:

$$l = 1 \text{ m};$$

$$Q = \text{diag}(100, 100, 100), R = 100;$$

$$u_{\max} = [-3.2 \text{ m/s} -0.5 \text{ rad}]^T, u_{\min} = [3.2 \text{ m/s} 0.5 \text{ rad}]^T;$$

$$\Delta u_{\min} = [-0.05 \text{ m/s} -0.47 \text{ rad}]^T, \Delta u_{\max} = [0.05 \text{ m/s} 0.47 \text{ rad}]^T;$$

$$\Gamma_{\min} = [-1 \text{ m} -1 \text{ m} -0.5 \text{ rad}]^T, \Gamma_{\max} = [22 \text{ m} 12 \text{ m} 0.5 \text{ rad}]^T;$$

$$\Delta \Gamma_{\min} = [-0.05 \text{ m} -0.05 \text{ m} -0.0082 \text{ rad}]^T,$$

$$\Delta \Gamma_{\max} = [0.05 \text{ m} 0.05 \text{ m} 0.0082 \text{ rad}]^T.$$  

(11)

5.2 Impact of speed on path tracking

The initial control parameters are set as $N_p=45, N_c=2, T=0.03 \text{ s}, v=1 \text{ m/s}, 2 \text{ m/s}, 3 \text{ m/s}$. In the navigation coordinate system, the trajectory tracking results are shown as Figure 6.

Figure 6 shows that the car tracks the reference path well at the speed of $3 \text{ m/s}$ or less. It can be seen from Figures 6b and 6c that the overshoot and adjustment time reach a maximum at the speed of $1 \text{ m/s}$ in transient response. The lateral tracking deviation reaches $7.51 \text{ cm}$ and the longitudinal tracking deviation reaches $-5.93 \text{ cm}$. The adjustment time and overshoot decrease with the increase of speed. This is because the regulation of the controller is earlier with faster speed. As a result, the overshoot is decreased.

Figure 6d, 6e verified the vehicle stability during the path tracking, the increase of speed has a great influence on the driving stability. When the speed is lower than $3 \text{ m/s}$, the higher the speed, the better the stability in transient response and the worse the stability in the running process. And the designed controller shows better performance during a straight-line path tracking.

5.3 Impact of sampling time on path tracking

The initial control parameters are set as $N_p=45, N_c=2, T=0.01 \text{ s}, 0.02 \text{ s}, 0.03 \text{ s}, v=3 \text{ m/s}$. In the navigation coordinate system, the trajectory tracking results are shown as Figure 7.

The control accuracy of nonlinear model prediction depends on the accuracy of the nonlinear prediction model. In this paper, the Euler method is used to solve the prediction model. Therefore, the accuracy of the prediction model is directly related to the...
sampling period T. It can be seen from Figure 7a, 7b that as the sampling period becoming larger, the variation of horizontal tracking deviation and vertical tracking deviation gradually becomes larger and the accuracy decreases.

Regarding the tracking stability, it is shown in Figure 7c and Figure 7d that the front wheel angle and speed are more stable with the longer sampling period in transient response. However, from nodes B, C, E, F on tracking path, the stability deteriorates when the sampling period becomes longer. This is due to a change in the trajectory equation, which requires the controller to re-predict the system parameters to get accommodated to the new path. In conclusion, an increase of the sampling period under the simulation condition will reduce the accuracy of the path tracking, at the same time it will improve the stability in the initial stage of driving and reduce the stability in the driving process.

5.4 Impact of lateral noise on path tracking

The initial control parameters are set as $N_p=45$, $N_c=2$, $T=0.03$ s, $v=3$ m/s, $Y_r=0.5$ m, 1 m, 1.5 m. In the navigation coordinate system, the trajectory tracking results are shown as Figure 8.

![Path tracking performance under different speed](image)

Figure 6  Path tracking performance under different speed
When unmanned vehicles deliver fruits, the vehicles need to perform the horizontal movement. The horizontal movement is taken as a disturbance for the system. The lateral deviation disturbance is injected at node D. As the disturbance increases, the tracking deviation and the adjustment time also increase. From Figure 8d and 8e, when the disturbance occurs, the controller will quickly respond to adjust the front wheel angle and speed so that the vehicle can back to the reference path as soon as possible.

6 Experiment and analysis

6.1 Path tracking test

The experiment takes place at Shandong Agricultural University. Test site has been shown as Figure 9.

The initial control parameters are set as $N_p=45$, $N_c=2$, $T=0.03$ s, $v=3$ m/s. To verify the robustness of the designed controller, lateral deviation disturbance $Y_r=0.5$ m, 1 m, 1.5 m to node D. The experiment result is shown in Figure 10.

It can be seen from Figure 10 that the off-track deviation of the straight line section is small. When tracking the circular section, the off-track deviation is large. The specific data as shown in Table 2.

The results illustrate that the test car can effectively track the
reference path with the nonlinear model predictive controller. The deviations mainly appear in the locations where the path curves change and the locations where the perturbations are added such as nodes C, D and F. As is shown in Table 2, the maximum lateral deviation is 13.36 cm and the maximum longitudinal deviation is 23.41 cm. There are mainly two reasons for the deviation. On one hand, experimental constraints: linkages between the various trailers, the delay of steering actuator, data transmission, and data processing. On the other hand, the reference trajectory changes occur at the end of the straight line path, where the car already has some cumulative deviation from the previous maneuvering process. The controller performs well over the straight section, which can be seen from the nodes B, E and G that the maximum lateral deviation is 9.01 cm and the maximum longitudinal deviation is 12.94 cm. It can be seen that the controller can meet the requirements of precision and stability of track tracking of agricultural vehicles.

6.2 Comparison with linear model predictive controller

In order to verify the proposed path-tracking controller, it is compared with the linear model predictive controller method in literature [36] in both the straight path and circular path. The main controller parameters are set \( N_p=45, N_a=2, T=0.03 \text{ s}, v=1 \text{ m/s}, \) \( 2 \text{ m/s}. \) The experimental results show that the two controllers have similar performance in the tracking accuracy when the velocity is less than 2 m/s. In the circular path tracking with speed \( v=3 \text{ m/s}, \) the test car under the linear model predictive controller showed a larger deviation. The average value of lateral off-track deviation was 12.06 cm and the average value of longitudinal tracking deviation was 38.04 cm. This is because the nonlinear characteristic of the car becomes prominent. The controller adopting a time-varying linear model as the predictive model demonstrates differences between the estimated trajectory and real trajectory. This will result in a larger tracking deviation. With the proposed controller, the average value of lateral off-track deviation is reduced by 36.8% and the average of longitudinal track deviation is reduced by 32.98%. Thus, at high speed, the controller has advantages in tracking accuracy.

7 Conclusions

(1) In this paper, nonlinear model predictive control of agricultural vehicles is proposed to tackle the low accuracy problem and poor prediction result from the linear model. The Euler method is used to establish the prediction model. Then the predictive control is transformed into quadratic programming problem based on recursive sequence. Finally, the nonlinear model is completed through feedback correction and rolling optimization. The design of the predictive controller is simulated and verified by experiments. It can be seen that the method is of less calculation complexity and high accuracy.

(2) This paper analyzes and tests the robust stability of agricultural vehicles emphatically. The results show that the controller can respond timely when the trajectory equation is changed or the disturbance is added, making the vehicle return to the reference track as soon as possible.

(3) From the field test results, when there is no disturbance and speed less 3 m/s, the maximum lateral tracking deviation is 13.36 cm and the maximum longitudinal tracking deviation is 23.41 cm. The automatic navigation of agricultural vehicles is basically realized. When adding maximum lateral deviation \( y_r=1.5 \text{ m}, \) the controller can quickly adjust the vehicle to go back to the reference trajectory. It is proved that the controller has strong robustness stability while keeping track precision.

Acknowledgements

This work is supported by Shandong Agricultural Machinery and Equipment Research and Development Innovation Initiative(2018YF020-07, 2017YF002), Modern Agricultural Technology System Innovation Team Post Project in Shandong Province (SDAIT-16-10), the National Key Research Projects (2017 YFD0700705), and the Natural Science Foundation of Shandong Province (ZR2019BC018).
[References]


